

Software for Calculating Viscosities of Molten Oxides

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GTT Technologies

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Outline

 **Motivation**

 **Urban-type viscosity models**

 **Software capabilities up to date**

 **Further Development**



Motivation

Behaviour of mineral matter is an important issue in coal utilisation processes

Slag viscosity is of particular importance for high temperature entrained flow gasifiers

Coal blending and fluxing are commonly used to maximise resource utilisation

The software is aimed

- to predict phase equilibrium for coal mineral matter at operational conditions
- to predict slag viscosity
- to assist in development of coal blending and fluxing strategies



Urbain Formalism

Urbain viscosity equation

$$\eta = AT \exp\left(\frac{1000B}{T}\right)$$

“Compensation Law”
(Theoretically derived)

$$-\ln A = mB + n$$

“Family” of liquids	m	n
Network oxides (SiO ₂ , GeO ₂)	0.154	13.24
Ionic liquids (Slags)	0.2981	11.15
Liquid metals	0.2188	12.612
Liquid salts	0.7232	12.405
H-bounded liquids (H ₂ O, methanol, etc.)	2.4296	11.396



Kalmanovich & Frank

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SiO₂-Al₂O₃-CaO-MgO

$$\eta = AT \exp\left(\frac{1000B}{T}\right)$$

$$\ln A = -(0.2812B + 11.8279)$$

$$B = B_0 + B_1 X_{SiO_2} + B_2 X_{SiO_2}^2 + B_3 X_{SiO_2}^3$$

$$B_0 = 13.8 + 39.9355\alpha - 44.049\alpha^2$$

$$B_1 = 30.481 - 117.1505\alpha + 129.9978\alpha^2$$

$$B_2 = -40.9429 + 234.0486\alpha - 300.04\alpha^2$$

$$B_3 = 60.7619 - 153.9276\alpha + 211.1616\alpha^2$$

$$\alpha = \frac{X_{CaO} + X_{MgO} + X_{FeO} + X_{Na_2O} + X_{K_2O} + 2X_{TiO_2}}{X_{CaO} + X_{MgO} + X_{FeO} + X_{Na_2O} + X_{K_2O} + 2X_{TiO_2} + X_{Al_2O_3}}$$



Kondratiev & Jak

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$\text{SiO}_2\text{-Al}_2\text{O}_3\text{-CaO- 'FeO'}$

$$\eta = AT \exp\left(\frac{1000B}{T}\right)$$

Separate B -values for different modifiers

Compositional dependence of the parameter m in

“Compensation Law” $m = m_A X_A + m_C X_C + m_F X_F + m_S X_S$

n	m_A	m_C	m_F	m_S
9.322	0.370	0.587	0.665	0.212

$$B_i = b_i^0 + b_i^1 \alpha + b_i^2 \alpha^2, \text{ where } \alpha = \frac{X_{Mod}}{X_{Mod} + X_{Amf}}$$



Kondratiev & Jak

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SiO₂-Al₂O₃-CaO-'FeO'

$$B = \sum_{i=0}^3 b_i^0 X_S^i + \sum_{i=0}^3 \sum_{j=1}^2 \left(b_i^{C,j} \frac{X_C}{X_C + X_F} + b_i^{F,j} \frac{X_F}{X_C + X_F} \right) \left(\frac{X_C + X_F}{X_C + X_F + X_A} \right)^j X_S^i$$

	<i>j/i</i>	0	1	2	3
b_i^0	0	13.31	36.98	-177.70	190.03
$b_i^{C,j}$	1	5.50	96.20	117.94	-219.56
	2	-4.68	-81.60	-109.80	196.00
$b_i^{F,j}$	1	34.30	-143.64	368.94	-254.85
	2	-45.63	129.96	-210.28	121.20



Comparison of the Models

$$\Delta = \frac{1}{N} \sum_{n=1}^N \left| \frac{(\eta_n)_{\text{calc}} - (\eta_n)_{\text{exp}}}{(\eta_n)_{\text{exp}}} \right|$$

System	Kalmanovich & Frank	Kondratiev & Jak
SiO ₂	99.9	19.1
Al ₂ O ₃ -SiO ₂	41.5	30.1
CaO-SiO ₂	24.3	10.9
'FeO'-SiO ₂	717.6	8.1
Al ₂ O ₃ -CaO-SiO ₂	24.6	31.2
CaO-'FeO'-SiO ₂	594.4	9.9
Al ₂ O ₃ -CaO-'FeO'-SiO ₂	169.6	29.2



Roscoe's Equation

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$$\eta_R = \eta_L (1 - RV_S)^{-n}$$

model parameters

First approximation:
rigid spheres of various sizes
→ $R=1$; $n=2.5$

Applicability range: $0 < V_s < 0.3$



NEW INTERACTIVE SOFTWARE: ViscCalc

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Based on the theoretical background outlined above a new interactive software has been developed.

It makes use of the viscosity models as described and integrates these with thermodynamic equilibrium calculations.

The equilibrium calculations are performed using GTT's own **Programmer's Library**

ChemApp™



Main Window

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VisCalc

File Settings

Variables

Name: a b

Values: 0;1;0.1 0;1-a;0.1

Liquidus Solidus

Calculations completed

Conditions

Temperature: 1500 [C]

Total pressure: 1 [atm]

Oxygen potential: 0.21 P(O₂)

Ash blend

	Amount in blend [moles]	Oxide Amounts in ash [moles]				
		SiO ₂	Al ₂ O ₃	CaO	Fe ₂ O ₃	FeO
Ash 1	a	1	0	0	0	0
Ash 2	b	0	1	0	0	0
Ash 3	1-a-b	0	0	1	0	0

Id	a	b	Temperature	Slag1_Viscosity	Slag2_Viscosity	Solids_volume_frac	Slurry_Viscosity
11	0	1	1500	NaN	NaN	1	NaN
12	0.1	0	1500	NaN	NaN	1	NaN
13	0.1	0.1	1500	0.640844242388...	NaN	0.291776756880...	1.518193219493.
14	0.1	0.2	1500	0.492598461488...	NaN	0	NaN
15	0.1	0.300000000000...	1500	0.779786690625...	NaN	0	NaN
16	0.1	0.4	1500	NaN	NaN	1	NaN
17	0.1	0.5	1500	NaN	NaN	1	NaN
18	0.1	0.600000000000...	1500	8.413667486817...	NaN	0.665708843438...	130.2186309137.
19	0.1	0.700000000000...	1500	12.97836630155...	NaN	0.716520174648...	303.3294909089.
20	0.1	0.8	1500	13.76728705925...	NaN	0.730623449149...	365.5517760974.
21	0.1	0.9	1500	NaN	NaN	1	NaN
22	0.2	0	1500	NaN	NaN	1	NaN
23	0.2	0.1	1500	0.683682665920...	NaN	0.261393606999...	1.458216180966.
24	0.2	0.2	1500	1.354241012756...	NaN	0	NaN
25	0.2	0.300000000000...	1500	NaN	NaN	1	NaN
26	0.2	0.4	1500	6.980257891824...	NaN	0.455054347471...	31.84113116556.
27	0.2	0.5	1500	8.413667461546...	NaN	0.341272622176...	23.89027002924.



Main Window (Input)

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The screenshot shows the VisCalc software interface. The window title is "VisCalc" and it has a menu bar with "File" and "Settings".

Variables

Name: a, b, [empty], [empty]
Values: 0;1;0.1, 0;1-a;0.1, [empty], [empty]

Calculations completed

Liquidus Solidus

Conditions

Temperature: 1500 [C]
Total pressure: 1 [atm]
Oxygen potential: 0.21 P(O₂)

Ash blend

	Amount in blend [moles]	Oxide Amounts in ash [moles]				
		SiO ₂	Al ₂ O ₃	CaO	Fe ₂ O ₃	FeO
Ash 1	a	1	0	0	0	0
Ash 2	b	0	1	0	0	0
Ash 3	1-a-b	0	0	1	0	0

Buttons: Calculate, Plot



Main Window (Table)

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Id	a	b	Temperature	Slag1_Viscosity	Slag2_Viscosity	Solids_volume_frac	Slurry_Viscosity
11	0	1	1500	NaN	NaN	1	NaN
12	0.1	0	1500	NaN	NaN	1	NaN
13	0.1	0.1	1500	0.640844242388...	NaN	0.291776756880...	1.518193219493.
14	0.1	0.2	1500	0.492598461488...	NaN	0	NaN
15	0.1	0.300000000000...	1500	0.779786690625...	NaN	0	NaN
16	0.1	0.4	1500	NaN	NaN	1	NaN
17	0.1	0.5	1500	NaN	NaN	1	NaN
18	0.1	0.600000000000...	1500	8.413667486817...	NaN	0.665708843438...	130.2186309137.
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21	0.1	0.9	1500	NaN	NaN	1	NaN
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23	0.2	0.1	1500	0.683682665920...	NaN	0.261393606999...	1.458216180966.
24	0.2	0.2	1500	1.354241012756...	NaN	0	NaN
25	0.2	0.300000000000...	1500	NaN	NaN	1	NaN
26	0.2	0.4	1500	6.980257891824...	NaN	0.455054347471...	31.84113116556.
27	0.2	0.5	1500	8.413667461546...	NaN	0.341272622176...	23.89027002924.



Main Window (Row)

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Results

Variables

{a = 3.000e-01} {b = 5.000e-01}

T [C] **P [atm]** **P(O2)**

1500.0 1.0 2.10e-01

Phases at Equilibrium

Corundum#1; Feldspar#1; Slag-liquid#1;

Blend composition [molar fractions]

SiO2	Al2O3	CaO	Fe2O3	FeO	Na2O
0.3	0.5	0.2	0	0	0

Slag Properties

	Temperature [C]	Viscosity [poise]	Slag Composition [molar fractions]					
			SiO2	Al2O3	CaO	Fe2O3	FeO	
Slag 1	1500.0	2.067e+01	0.39507	0.298	0.30693	0	0	
Slag 2	1500.0	Slag 2 is not formed at these conditions!						
Liquidus	1774.0	2.698e+00	0.3	0.5	0.2	0	0	
Solidus	1446.5	2.332e+01	0.37459	0.28096	0.34445	0	0	

Comments:

The volume fraction of solids is above the applicability range for Roscoe's equation

Volume fraction of solids

0.5457

Viscosity of slurry

1.486e+02

Primary phase

Corundum#1

View Table
Previous
Next



Axes Selection

Plot Settings

Axes

Property	X	Y1	Y2	Series Name
Liquidus_temperature	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	Liquidus_temperature
Liquidus_Viscosity	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	
Solidus_Temperature	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	Solidus_Temperature
Solidus_Viscosity	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	

Plot Title Liquidus and Solidus vs Composition

X-Axis Title Silica mole fraction

Y1-Axis Title Liquidus

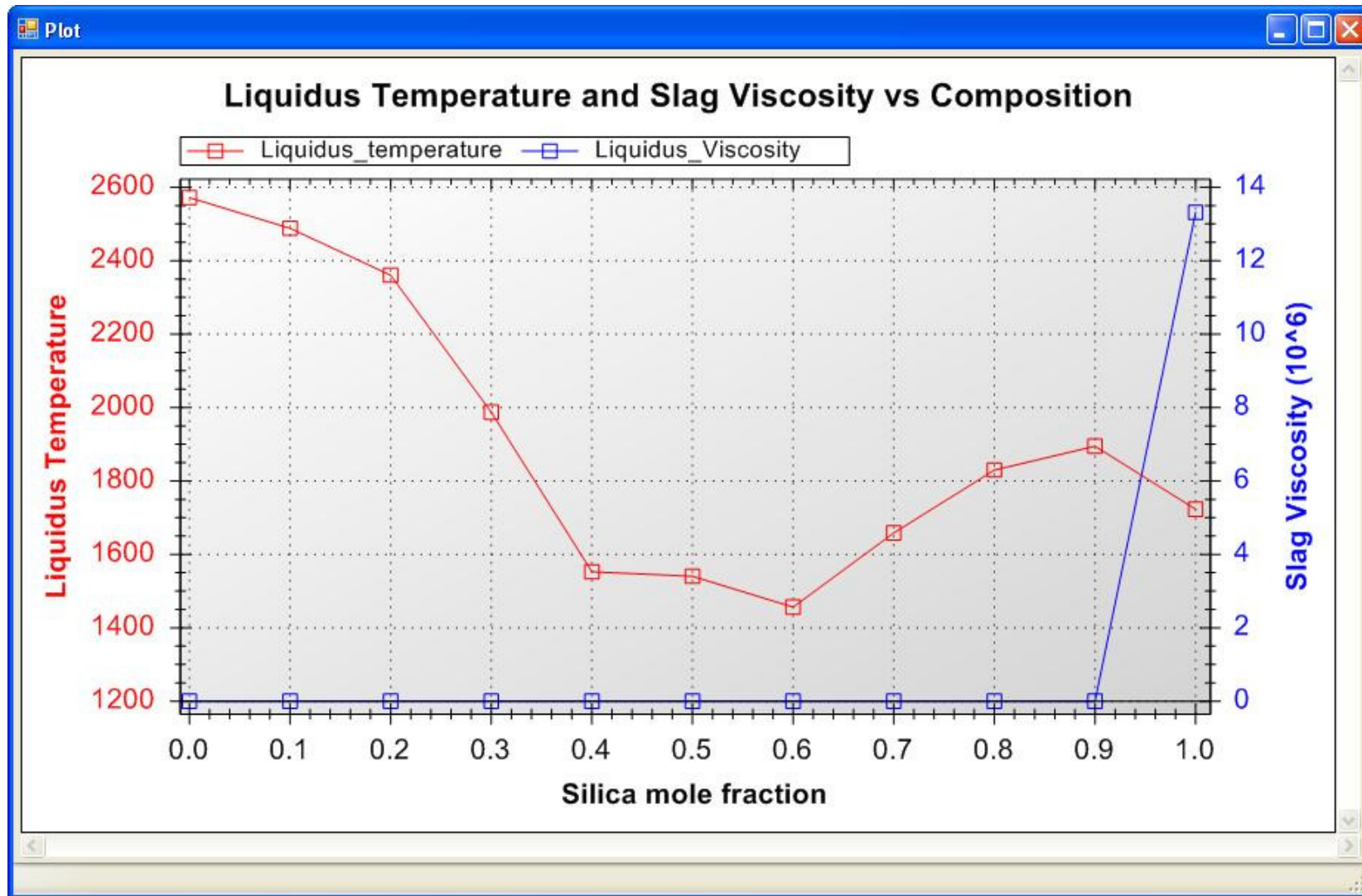
Y2-Axis Title Solidus

Display Plot



Plotting

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Demonstration



Further Development

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- **New viscosity models (Avramov)**
- **Plotting capabilities (Ternary diagrams)**
- **Bulk calculations (Imported tables)**
- **?**



Avramov vs Arrhenius

Avramov

$$\eta = \frac{\eta_0}{\sum X_i \exp(-E_i/RT)}$$

average

jump frequency

Concentrations of SU

Constant

Activation energies of SU

Arrhenius

$$\eta = \eta_0 \exp(\sum X_i E_i / RT)$$

average

activation energy



Avramov vs Arrhenius

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The system $\text{Na}_2\text{O}-\text{SiO}_2$, 1200°C

